



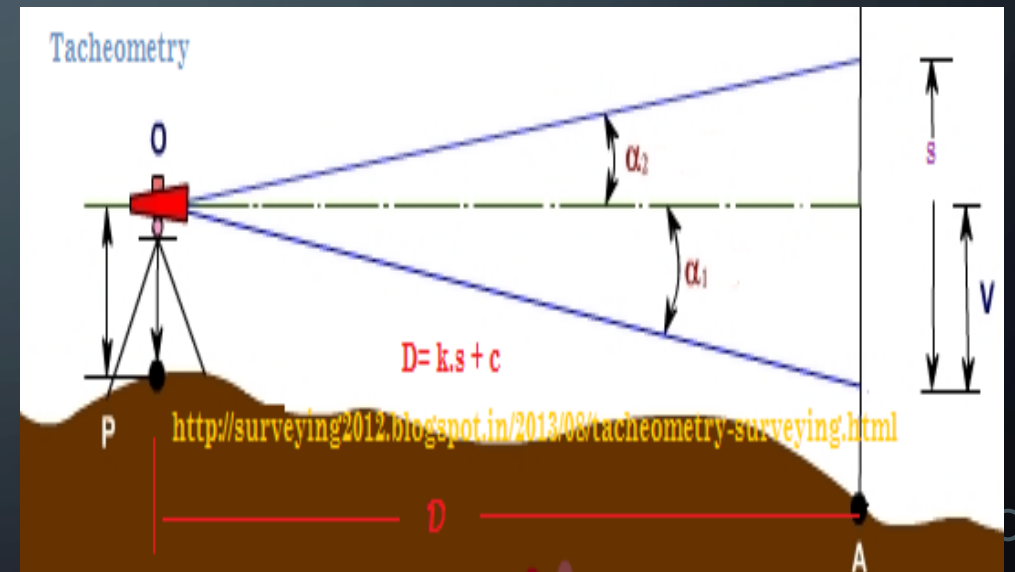
TACHEOMETRY

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INTRODUCTION

- Tacheometry- branch of angular surveying in which the horizontal distances from the instrument station to the staff and vertical distances of points are determined from instrumental observation
- Chaining is completely eliminated
- Adopted in rough and difficult terrain
- Purpose
 - Preparation of contour maps
 - Used in hydrographic survey
 - Location survey of roads, railways, reservoirs etc
 - Used for accurate measurements



PRINCIPLE

- To enable horizontal & vertical distances to be computed from readings upon a stadia rod & thus eliminate the chaining operation
- Statement — In isosceles triangles, ratio of the perpendiculars from vertex on their bases is constant

$$\frac{AO}{BC} = \frac{AO'}{B'C'} = 2 \cot \frac{\alpha}{2} = K$$

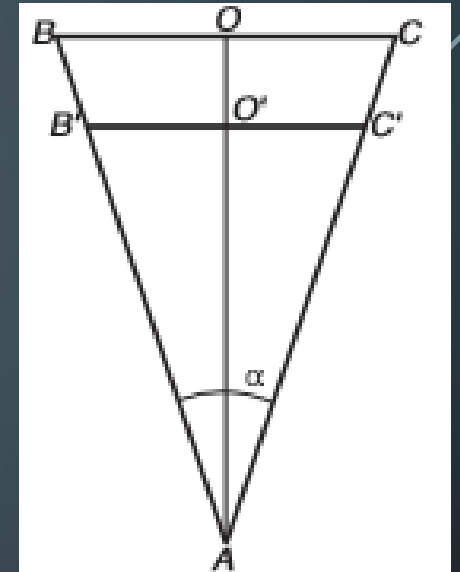
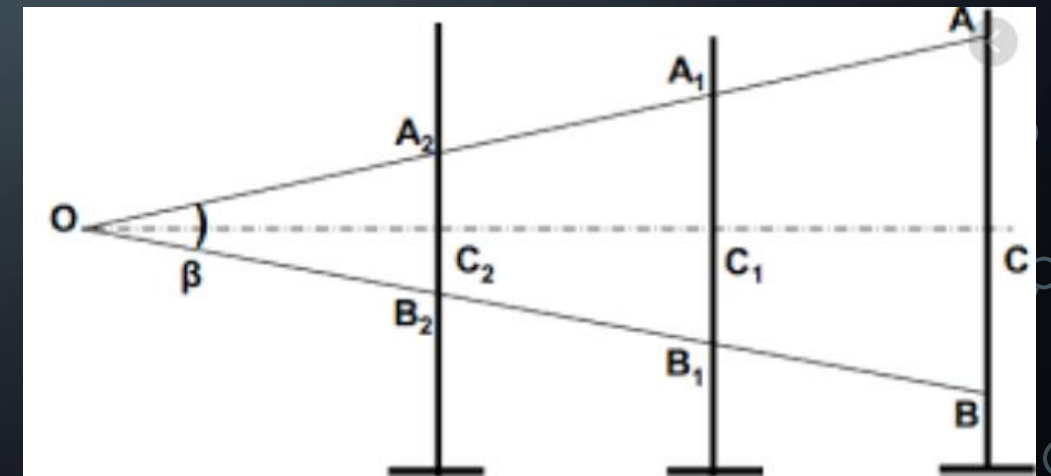
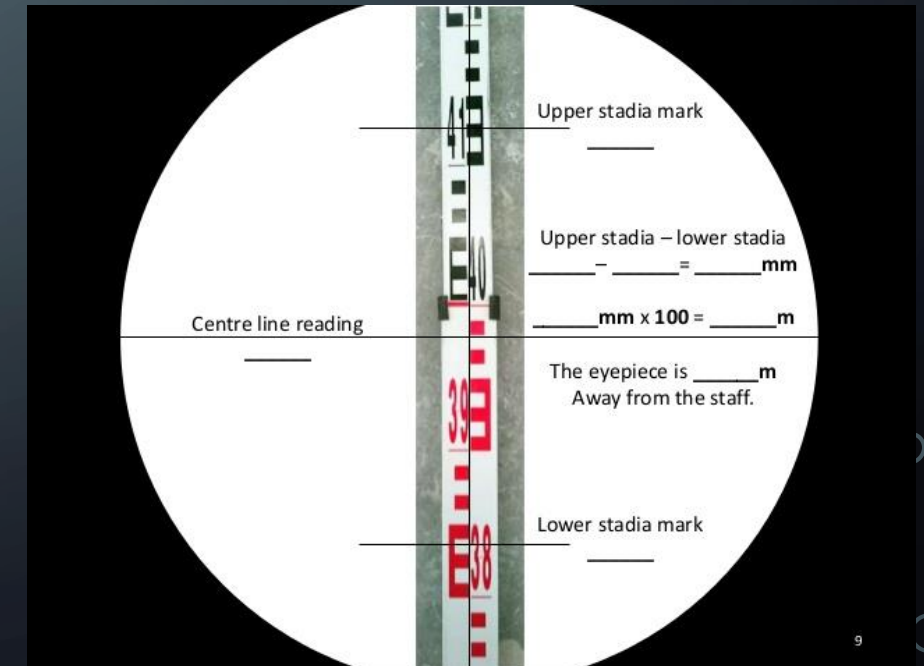
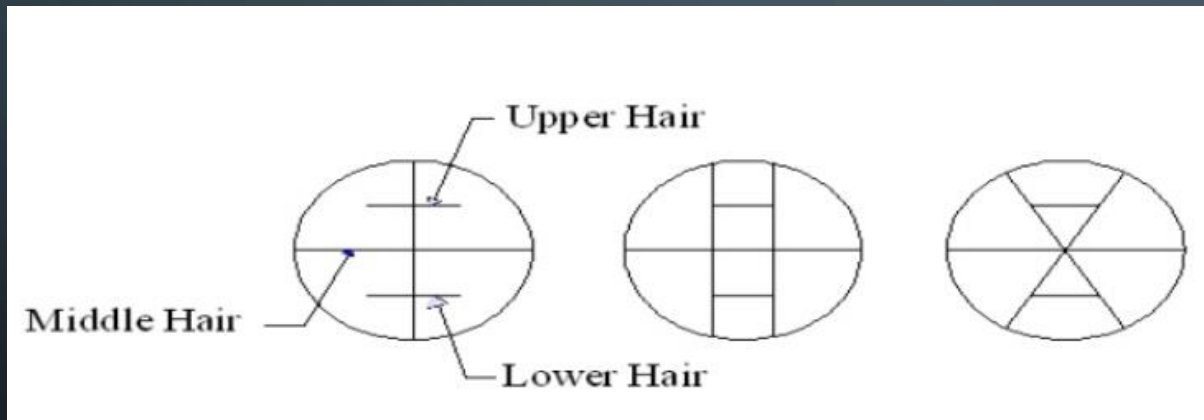


Fig. 13.2. Principle of tacheometry.



INSTRUMENTS

- Tacheometer – transit theodolite with stadia diaphragm
- Stadia rods



DIFFERENCE BETWEEN THEODOLITE & TACHEOMETER

Theodolite

- It is used for measurement of horizontal & vertical angle.
- In theodolite survey , distances are measured by chain or tape.
- Suitable for plane & hilly area with less obstacles.
- More stations are required in theodolite survey.

Tacheometer

- It is used for measurement of horizontal & vertical distances.
- In tacheometric survey ,direct measurement of distances are possible.
- Suitable in case obstacles like river broken ground.
- Less stations are required in tacheometric survey.

TACHEOMETRIC CONSTANTS

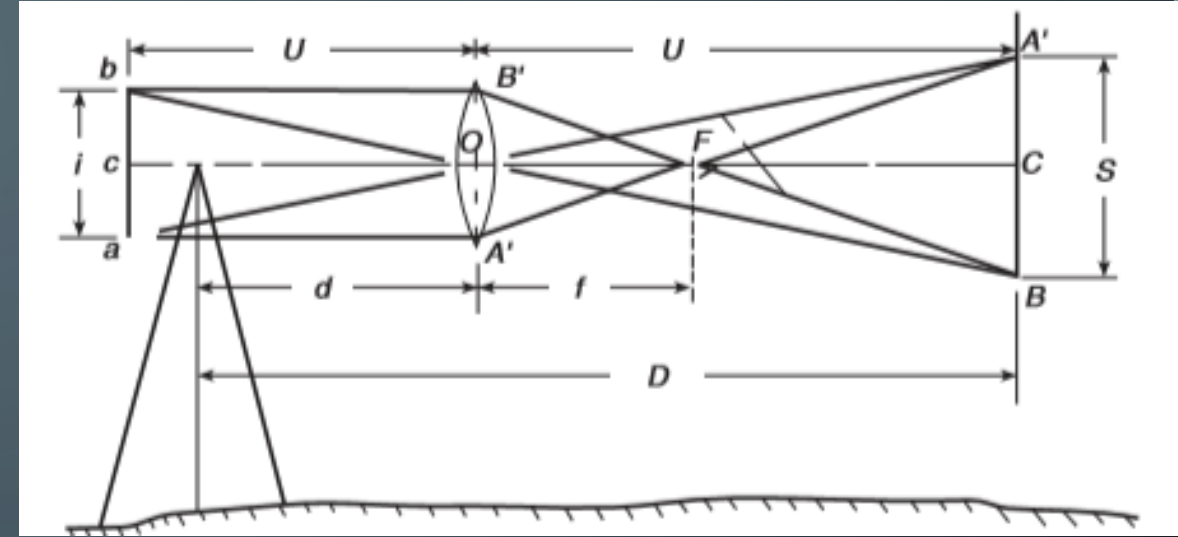
- Multiplication constant, $A (=f/i)$
- Additive constant, $B (=f+d)$

where, f = focal length of image glass

i = length of image (stadia hair interval)

d = horizontal distance from optical center of object glass to vertical axis of tacheometer

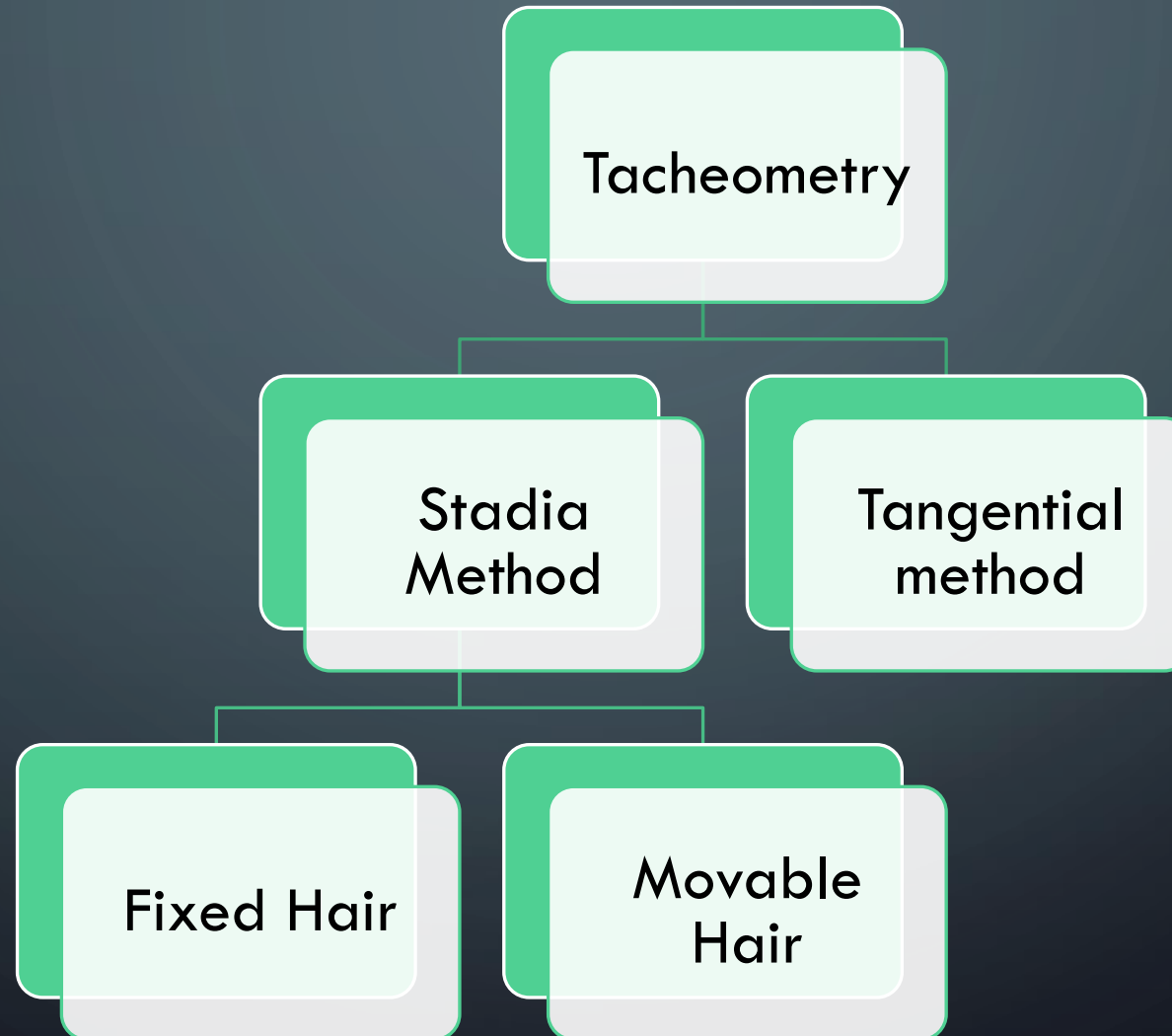
Note: if fitted with an anallatic lens, additive constant = 0



REQUIREMENTS OF A TACHEOMETER

- Multiplying constant = 100 & error in the computed distance should not exceed 1 in 1000
- Central hair reading should be exactly midway between the stadia hair
- Telescope must be truly anallatic, i.e., additive constant = 0
- Telescope should be powerful having a magnification of 20 to 30 diameters

TACHEOMETRIC METHODS



The image features a dark blue gradient background. In the corners, there are decorative white line art elements resembling circuit boards or neural networks, with lines and small circles connecting them.

STADIA METHOD

FIXED HAIR METHOD

- Distance between stadia hairs is fixed
- Intercept on levelling staff varies
- Staff intercept (s)– difference between upper and lower stadia hair readings
- Method suitable for horizontal & inclined sights
- For inclined sights staff readings may be taken with staff vertical or normal to the line of sight
- Most common method

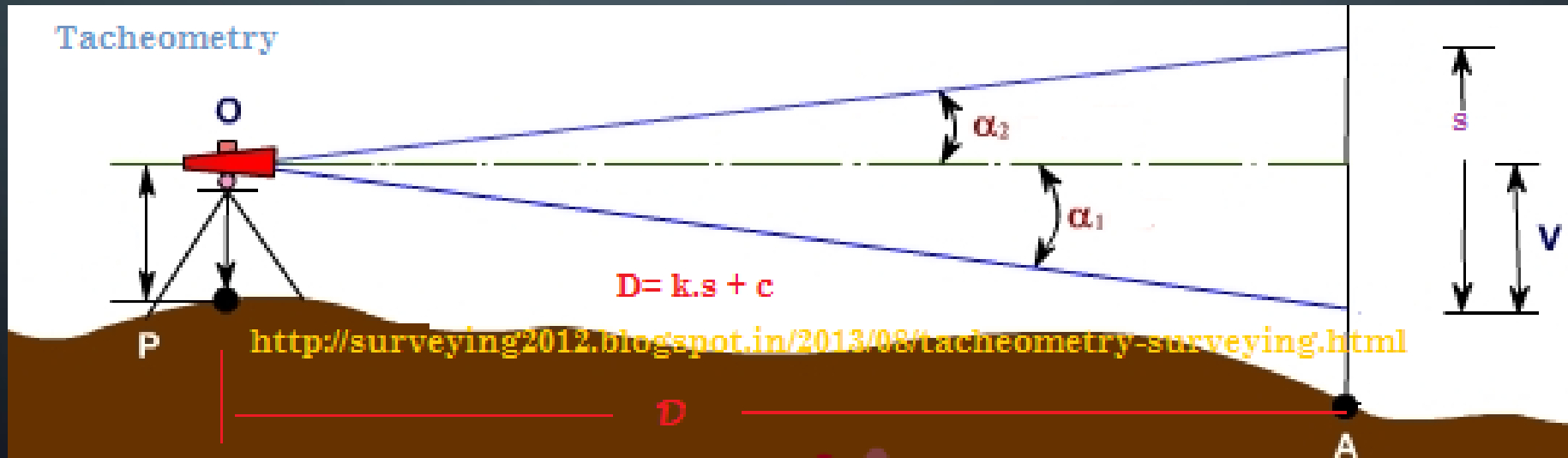
FIXED HAIR METHOD - CASES

- Three cases

1. Line of sight is horizontal & staff is held vertical
2. Line of sight is inclined & staff is vertical
3. Line of sight is inclined & staff is held normal to the line of sight

1. LINE OF SIGHT HORIZONTAL

- Horizontal distance $D = As + B$, where s - staff intercept
- RL of staff station = HI – Central hair reading
- HI = RL of BM + BS



2. LINE OF SIGHT INCLINED; STAFF VERTICAL

Horizontal distance, $D = A \cos^2 \theta + B \cos \theta$

Elevation formula:

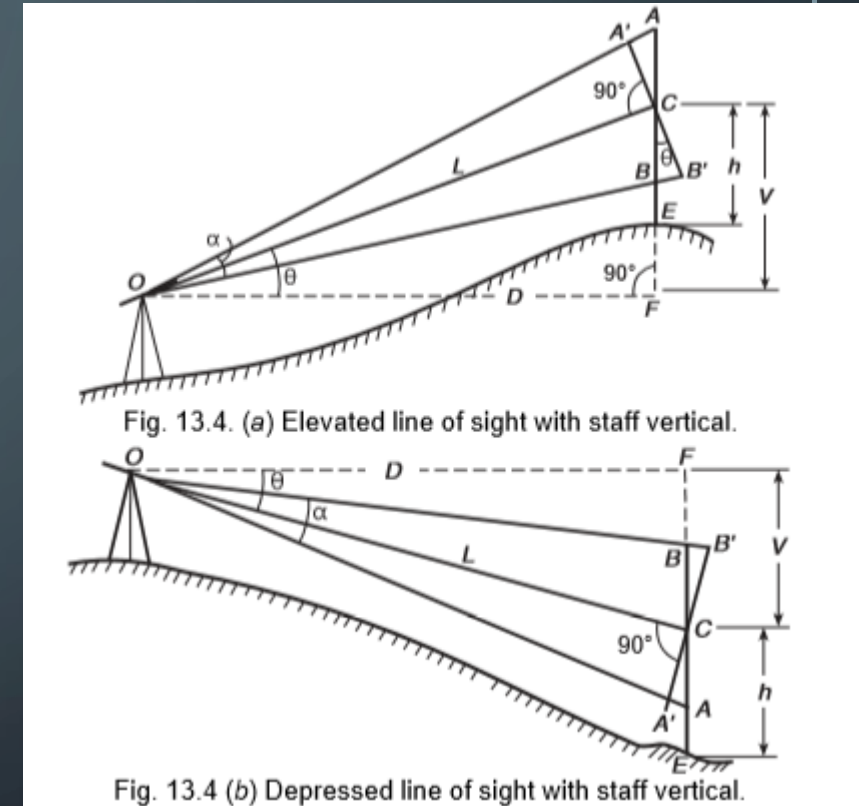
$$V = A \sin \frac{2\theta}{2} + B \sin \theta$$

For angle of elevation:

RL of staff station = HI + V-h, h- central hair reading

For angle of depression:

RL of staff station = HI - V-h



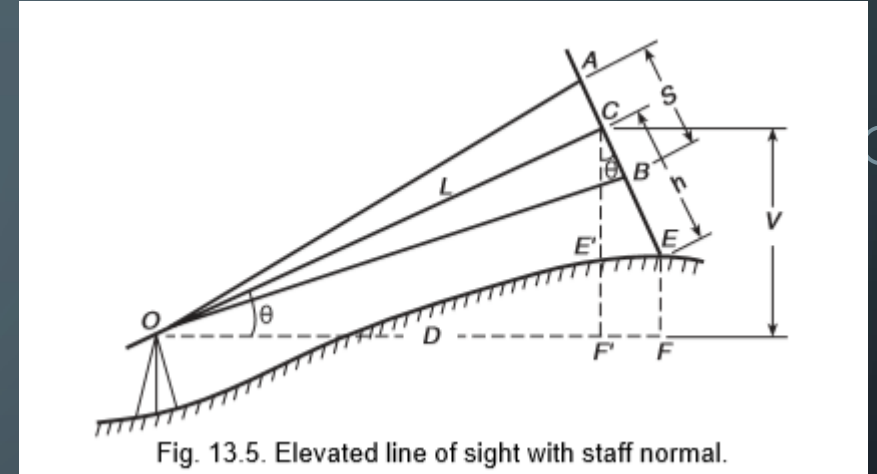
3. LINE OF SIGHT INCLINED; STAFF NORMAL

A. For angle of elevation

Horizontal distance, $D = (As+B) \cos\theta + h \sin\theta$

$V = (As+B) \sin\theta$

RL of staff station = HI + $V - h \cos\theta$

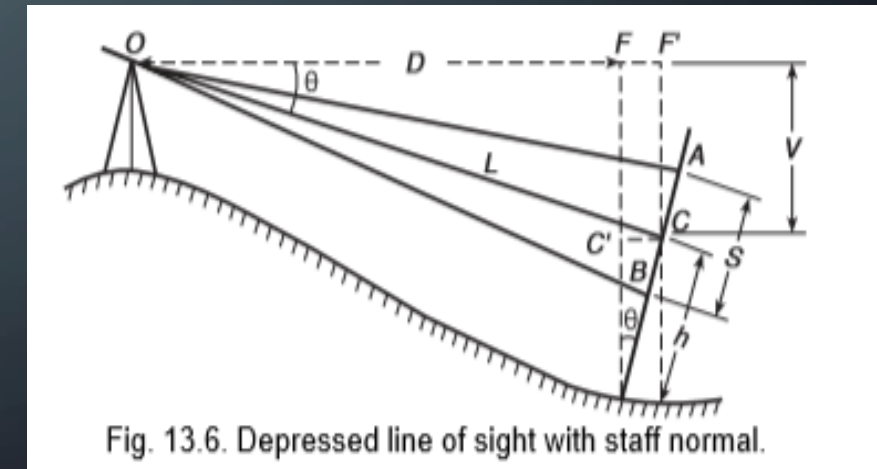


B. For angle of depression

Horizontal distance, $D = (As+B) \cos\theta - h \sin\theta$

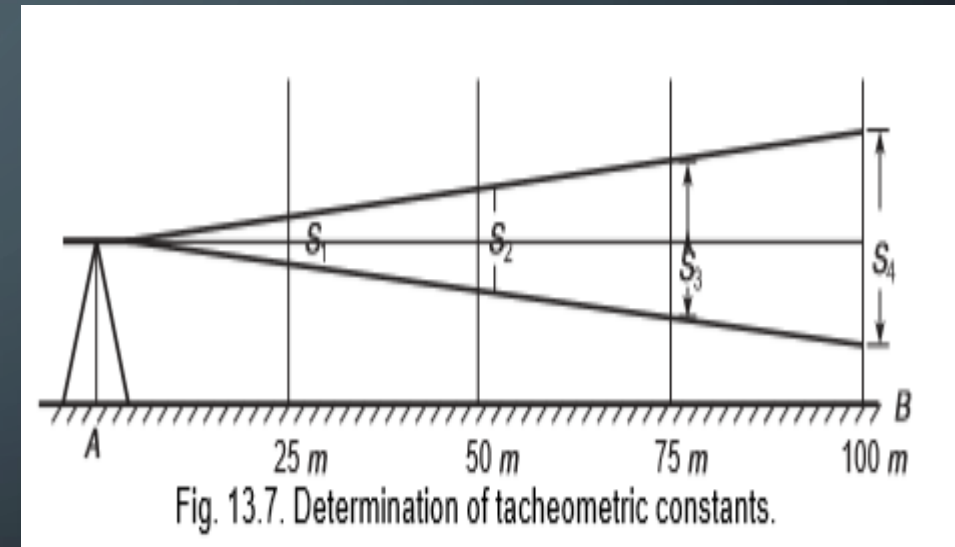
$V = (As+B) \sin\theta$

RL of staff station = HI - $V - h \cos\theta$



DETERMINATION OF TACHEOMETRIC CONSTANTS

- Measure line AB 100 m long on a fairly level ground and fix pegs at 25 m interval
- Set up instrument at A and centre it
- Obtain staff intercepts s_1 , s_2 , s_3 and s_4
- Substitute the different values of D and s in the equation, $D = As+B$, to get 4 quadratic equations
- Solve the equations in pair to get the values of tacheometric constants and take its mean



Q1)

Example 13.2. A staff was held vertically at a distance of 46.2 m and 117.6 m from the centre of a theodolite fitted with stadia hairs and the staff intercepts with the telescope horizontal were 0.45 m and 1.15 m respectively. The instrument was then set over a station P of RL. = 150 m, the height of instrument axis being 1.38 m. The stadia hair readings on a staff held vertically at a station Q were 1.2 m, 1.93 m and 2.65 m respectively, while the vertical angle was $-9^\circ 30'$. Find the distance PQ and RL. of Q.

Step 1: Calculation of tacheometric constants

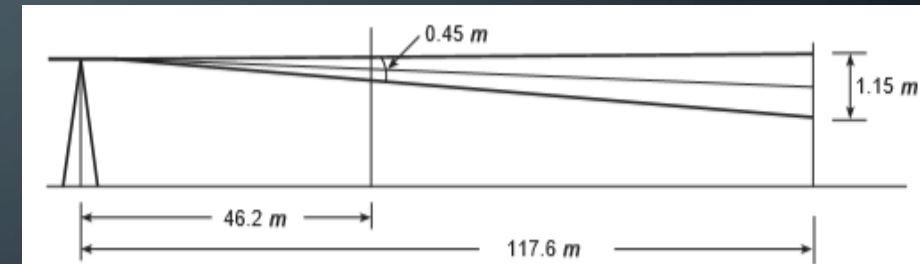
Substituting the values in eqn, $D = As+B$ we get

$$46.2 = A \times 0.45 + B$$

$$117.6 = A \times 1.5 + B$$

On solving these two eqns, we get

$$A = 102, B = 0.3$$



Step 2: Calculation of distance PQ & RL of Q

Horizontal distance, $PQ = A \cos^2 \theta + B \cos \theta$

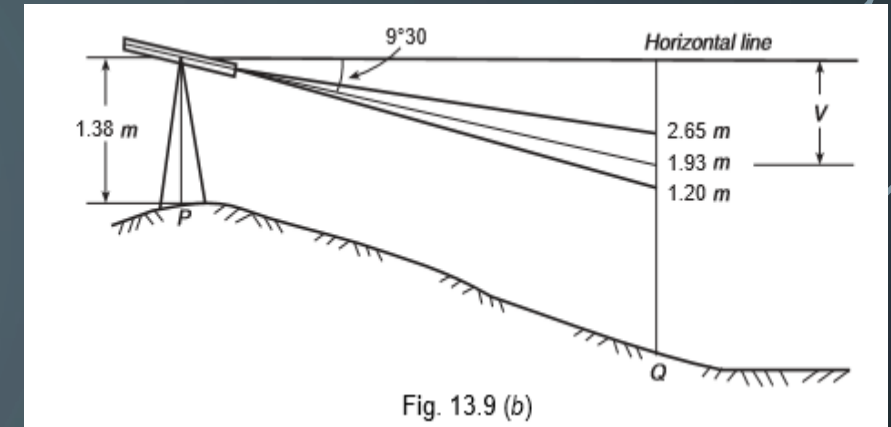
$$s = 2.65 - 1.20 = 1.45 \text{ m}$$

$$\theta = 9^\circ 30'$$

Substituting the values in above eqn, we get, $PQ = 144.17 \text{ m}$

$$\begin{aligned} \text{Vertical Component, } V &= A s \frac{\sin 2\theta}{2} + B \sin \theta \\ &= 24.13 \text{ m} \end{aligned}$$

$$\begin{aligned} \text{RL of Q} &= \text{RL of P} + \text{height of line of sight} - V - h \\ &= 150 + 1.38 - 24.13 - 1.93 \\ &= 125.32 \text{ m} \end{aligned}$$



Q2)

Example 13.4. A tacheometer was set up at an intermediate station *C* of the line *AB* and following readings were obtained :

<i>Staff Station</i>	<i>Vertical angle</i>	<i>Staff readings</i>		
<i>A</i>	$-6^{\circ} 20'$	0.445	1.675	2.905
<i>B</i>	$+4^{\circ} 20'$	0.950	1.880	2.810

The instrument was fitted with an anallatic lens and the constant was 100. Find the gradient of the line joining station *A* and station *B*.

Step 1: staff held at A

$$s_1 = 2.905 - 0.445 = 2.460 \text{ m}; \theta_1 = -6^{\circ} 20'$$

$$\begin{aligned} \text{Distance CA} &= A \cos^2 \theta + B \cos \theta \\ &= 243 \text{ m} \end{aligned}$$

$$\begin{aligned} \text{Vertical Component V1} &= A \sin \frac{2\theta}{2} + B \sin \theta \\ &= 26.971 \text{ m} \end{aligned}$$

Step 2: staff held at B

$$s_2 = 1.860 \text{ m}; \theta_2 = 4^\circ 20'$$

$$\begin{aligned}\text{Distance CB} &= A \cos^2 \theta + B \cos \theta \\ &= 184.94 \text{ m}\end{aligned}$$

$$\begin{aligned}\text{Vertical Component } V_2 &= A s \frac{\sin 2\theta}{2} + B \sin \theta \\ &= 14.014 \text{ m}\end{aligned}$$

$$\text{Distance AB} = \text{CA} + \text{CB} = 427.94 \text{ m}$$

Step 3: Calculation of Gradient

Let X be the RL of trunnion axis

$$\text{RL of A} = X - V_1 - h_1 = X - 26.71 - 1.675 = X - 28.646$$

$$\text{RL of B} = X + V_2 - h_2 = X + 14.014 - 1.880 = X + 12.134$$

$$\text{Difference in elevation} = \text{RL of B} - \text{RL of A} = 40.780 \text{ m}$$

$$\text{Gradient of line AB} = \frac{\text{Horizontal distance}}{\text{Difference in level}} = 1 \text{ in } 10.49$$

Q3)

Example 13.5. Determine the gradient from a point A to a point B from the following observations made with a fixed hair tacheometer fitted with an anallatic lens, the constant of the instrument being 100.

	Bearing	Reading of stadia hairs	Reading of axial hair	Vertical angle
To A	345°	0.750 2.120	1.435	+15°
To B	75°	0.625 3.050	1.835	+10°

Let the instrument station be T

$s_1 = 1.370$ m, $s_2 = 2.425$ m

Distance TA = $A \cos^2 \theta + B \cos \theta = 127.82$ m

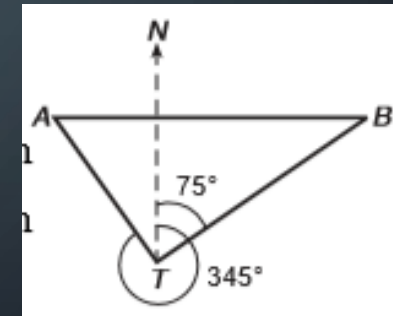
Distance TB = 235.19 m

Angle ATB = Bearing of TB – Bearing of TA = 90°

Distance AB = $\sqrt{TA^2 + TB^2}$
= 267.68 m

Note, Distance formula:

$$PQ^2 = OP^2 + OQ^2 - 2 OP \cdot OQ \cos POQ$$



Vertical Components

$$V1 = 34.25 \text{ m}$$

$$V2 = 41.47 \text{ m}$$

Let X be the RL of trunnion axis

$$\text{RL of A} = X + V1 - h1$$

$$\text{RL of B} = X + V2 - h2$$

$$\begin{aligned} \text{Difference in elevation between B and A} &= \text{RL of B} - \text{RL of A} \\ &= 6.820 \text{ m, B being higher} \end{aligned}$$

$$\text{Gradient} = 1 \text{ in } 39.25$$

Q4)

Example 13.12. In a tacheometer survey made with an instrument whose constants are 100 and 0.5, the staff was inclined so as to be normal to the line of sight for each reading. Two sets of readings were as given below. Calculate the gradient between the staff stations P and Q and the reduced level of each if that of R is 41.800 m.

Instrument Station	Height of Instrument Axis	Staff Station	Bearing	Vertical Angle	Stadia Reading
R	1.600	P	85°	+ 4° 30'	1.000 1.417 1.833
		Q	135°	− 4° 00'	1.000 1.657 2.313

(a) Staff Station P

Staff interval $S_1 = 1.833 - 1.000 = 0.833$ m

Central wire reading = 1.417 m

Substituting the values of S and θ in Eqns. (i) and (ii), we get

$$\begin{aligned}
 H_1 &= (100 \times 0.833 + 0.5) \cos 4^\circ 30' + 1.417 \times \sin 4^\circ 30' \\
 &= 83.8 \times 0.996917 + 1.417 \times 0.0784592 \\
 &= 83.54 + 0.11 \\
 &= 83.65 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 \text{and } V_1 &= (100 \times 0.833 + 0.5) \sin 4^\circ 30' \\
 &= 83.8 \times 0.07846 \\
 &= 6.575 \text{ m.} \quad \dots(ii)
 \end{aligned}$$

$$\begin{aligned}
 \therefore \text{Ground level at } P &= 41.800 + 1.600 + 6.575 - 1.417 \cos 4^\circ 30' \\
 &= 41.800 + 1.600 + 6.575 - 1.413 \\
 &= 48.562 \text{ m}
 \end{aligned}$$

(b) Staff Station Q

Staff interval $S_2 = 2.313 - 1.000 = 1.313$

Central wire reading = 1.657

Substituting the values of S and θ , in Eqs. (i) and (ii), we get

$$\begin{aligned}H_2 &= (100 \times 1.313 + 0.5) \cos 4^\circ - 1.657 \sin 4^\circ \\&= 131.8 \times 0.997564 - 1.657 \times 0.06976 \\&= 131.48 - 0.12 = 131.36 \text{ m}\end{aligned}$$

$$\begin{aligned}V_2 &= 131.8 \sin 4^\circ = 131.8 \times 0.0697566 \\&= 9.194 \text{ m}\end{aligned}$$

$\therefore$ Ground level at

$$\begin{aligned}Q &= 41.800 + 1.600 - 9.194 - 1.657 \times \cos 4^\circ \\&= 41.800 + 1.600 - 9.194 - 1.653 \\&= 32.553 \text{ m}\end{aligned}$$

Difference in level of P and $Q = 48.562 - 32.553 = 16.009 \text{ m}$

Angle $PRQ = \text{Bearing of } RQ - \text{Bearing of } RP = 135^\circ - 85^\circ = 50^\circ$

Applying cosine formula to $\triangle RPQ$, we get

$$\begin{aligned}PQ^2 &= (83.65)^2 + (131.36)^2 - 2 \times 83.65 \times 131.36 \cos 50^\circ \\&= 69,97.32 + 172,55.45 - 2 \times 479.46 \times 0.642788 \\&= 10126.520\end{aligned}$$

$PQ = 100.63 \text{ m.}$

The gradient between P and Q

$$\begin{aligned}&= \frac{100.63}{48.562 - 32.553} \\&= \frac{100.63}{16.009} = 1 \text{ in } 6.286 \text{ fall.}\end{aligned}$$

Q5)

Example 13.1. *A tacheometer has a diaphragm with three cross hairs spaced at distances 1.15 mm. The focal length of the object glass is 23 cm and the distance from the object glass to the trunnion axis is 10 cm. Calculate the tacheometric constants.*

$$i = 2 \times 1.15 = 2.30 \text{ mm} = 0.23 \text{ cm}$$

$$A = \frac{f}{i} = \frac{23}{0.23} = 100$$

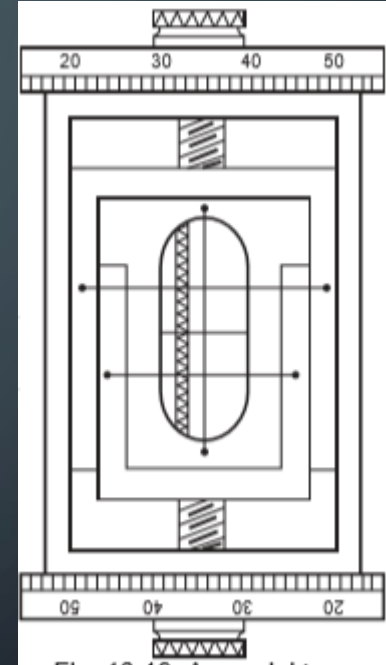
$$B = (f + d) = (23 + 10) = 33 \text{ cm} = 0.33 \text{ m}$$

MOVABLE HAIR METHOD

- Stadia interval is variable
- Instrument is fitted with a stadia diaphragm which can be moved
- Staff intercept kept constant
- In this method, variable stadia interval is measured first. From this, horizontal distance is calculated
- This method is not commonly used

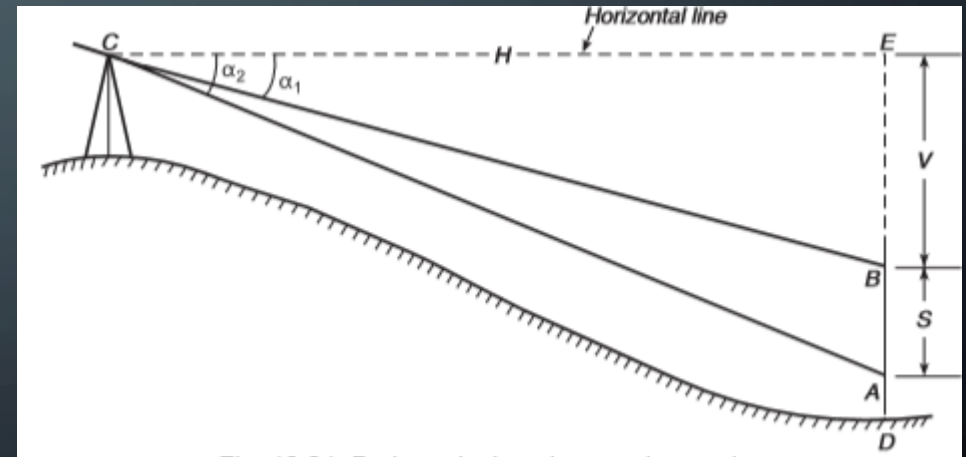
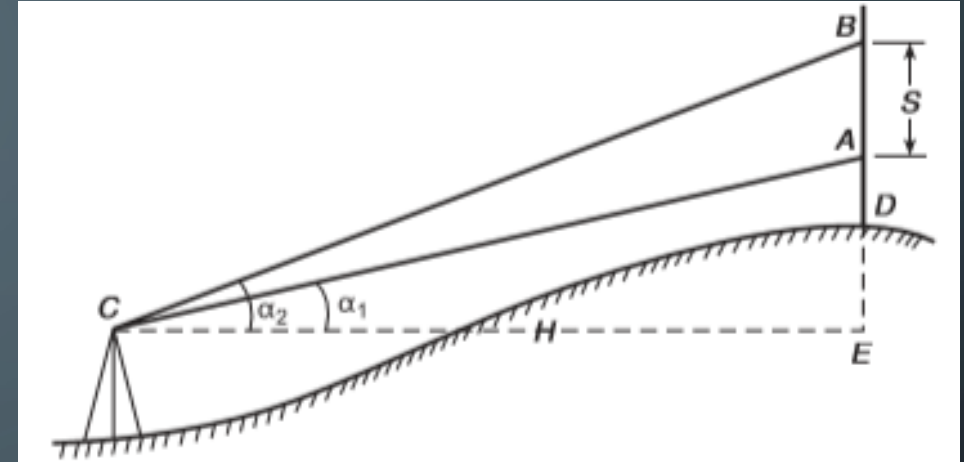
- Distance formula,
$$D = \frac{A}{m} S + B$$

where m is the number of revolutions of the micrometer of pitch p



TANGENTIAL METHOD

- When telescope is not fitted with stadia diaphragm, then tangential method is preferably adopted
- In this method, a staff is fitted and provided with two targets at fixed distance apart and the vertical angles to the two vanes are taken
- Then horizontal distance and RLs are calculated



RADIAL CONTOURING

- In case of hilly areas, radial contouring method is adopted
- Tacheometer is set at a point approximately at the centre of the area.
- Radial lines are set making angles with either the magnetic meridian or with the first radial line
- On each radial line staff readings are observed at different points
- When all radial line observations are taken, it is then plotted on a sheet to a suitable scale

